

# Eclipsing binary systems with eccentric orbits

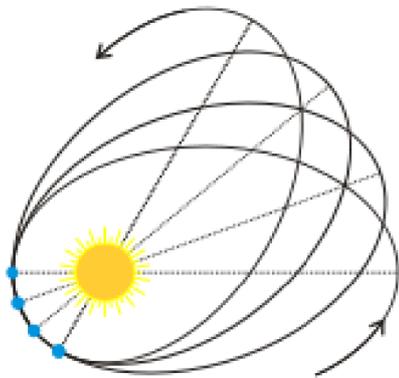
*Eccentric eclipsing binaries are a subgroup of detached binary stars that have provided new and important information for the study of internal stellar structure. Eccentric systems display the phenomenon of Apical motion. In particular, apical motions in this type of binary systems has proven to be highly rewarding during the past decades, allowing to get valuable astrophysics parameters of the binary system.*

Currently there are more than a hundred eccentric eclipsing systems known. Many of them still require extensive observations for creation of reliable astrophysical models of their systems. Below one can read a short overview of this kind of systems and their examples

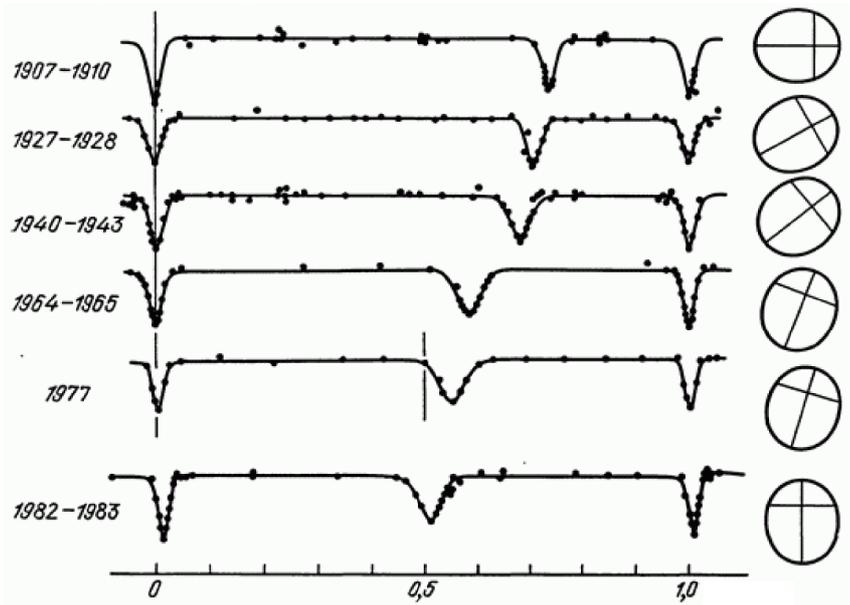
## The apical motion effect

The study of apical motion effect in detached eclipsing binary systems with eccentric orbits (EEB) is an important source of information on the stellar internal structure as well as for the possibility of verification of the theory of General Relativity

periastron of binary stars in order to have some insight into their internal structure was given by Russell (1928). In eccentric binaries, the behavior of the orbit is influenced by the distortion of the components. This is a function of the internal



**Fig.1.** The light curve evolution of RU Mon between 1907 and 1983, due to the apical motion effect (right). Schematic model of the line of apsides rotation (top).



(Claret & Gimenez 1993; Claret 1997). It is the rotation of the line of apses of the orbit of an eccentric or elliptical two body system. The rate of motion of the apsis is dependent on the internal structure of each component. Determination of the characteristics of a binary thus provides an observational test of the theory of stellar structure and evolution.

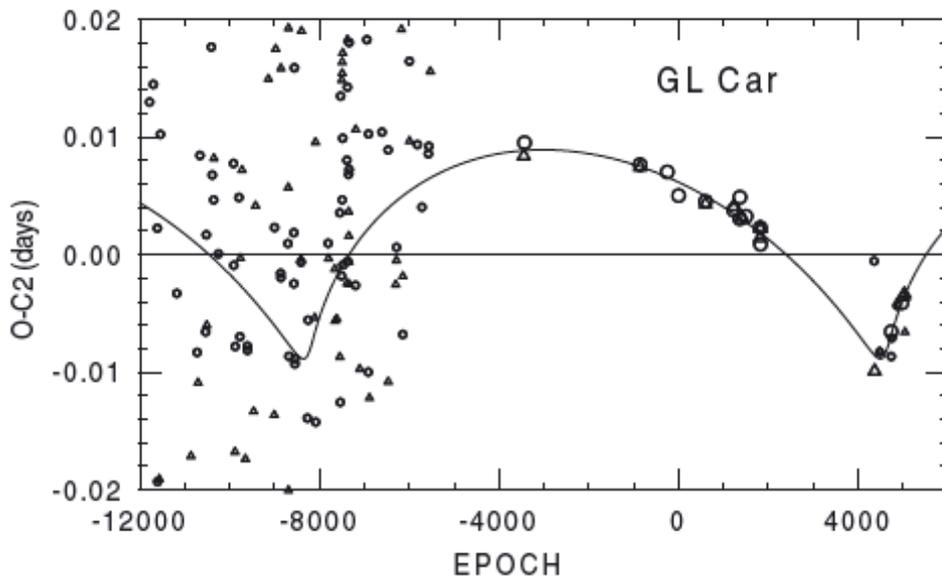
The first theoretical explanation of apical motion (the precession of an eccentric orbit in its own plane) extends back to the beginning of the 20th century. The history of apical motion studies based on observations of times of minima of eclipsing binary stars is long and interesting. It began with the recognition by Dunér (1892) that there were two separate types of minima of Y Cyg with significantly different periods, and he correctly attributed this effect to a rotating line of apsides. This massive binary is one of the best-known cases of apical motion among eclipsing binaries.

density concentration as well as the mass ratio and the separation of the components. Stellar distortion, or deviation from the point-like behavior, is responsible for the secular movement of the periastron and its observational measurement should obviously lead to an empirical measurement of the level of the density concentration. A fairly good historic introduction can be found in (Gimenez, 2006).

From the observational point of view, the study of this effect requires a more or less continuous monitoring of times of minimum light of the candidate systems. The necessarily long time basis of the observations requires a careful preparation of programs and targets.

This means that a large amount of observing time is generally needed which is not available at large instruments. Since only accurate timings of relatively deep eclipses are needed, a moderate or even small telescopes equipped with a photoelectric photometer or a CCD camera can be perfectly suited to this kind of project.

The initial idea to measure the motion of the



**Fig. 2.** The  $O-C_2$  diagram for the times of minima of GL Car after subtraction of the apsidal motion. The curve represents a light-time effect for the possible third body eccentric orbit with a period of about 90 yr and an amplitude of about 13 min. The individual primary and secondary minima are denoted by circles and triangles, respectively (Wolf et al., 2008).

There are some advantages and disadvantages of the use of this effect (Hegedüs et al. 2005):

Advantages:

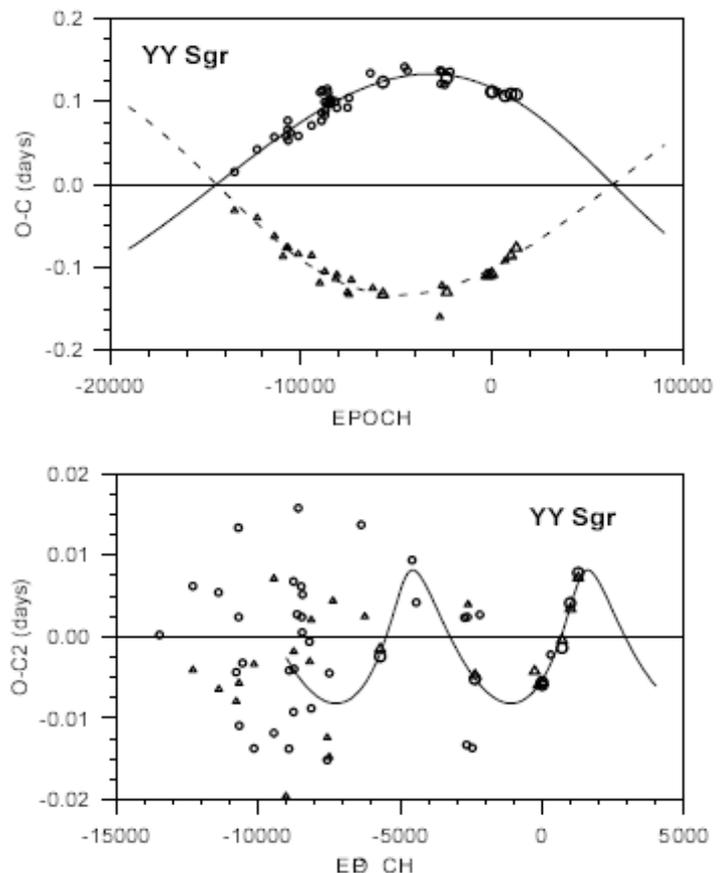
- its basic study requires only very simple techniques (timing of eclipsing minima).
- the effect includes information not only about the internal mass distribution, but the gravitational theory itself as well.

Disadvantages:

- generally one needs to wait for quite a long time until the effect can be revealed;
- by the study of minima time observations (or by changes in the spectroscopic orbital elements), because the typical periods of this effect are from several hundred to several thousand years;
- the individual internal structure parameters remain unknown, only the weighted average of the two components can be determined.

A detailed analysis of the period variations can be performed using times of minimum light observed throughout the apsidal motion cycle, and from this both the orbital eccentricity and the period of rotation of the periastron can be obtained with a high accuracy. Moreover, this provides independent information for the analysis of the light curves (Giménez, 1994).

Similar photometric studies of apsidal motion in EEB's were published regularly during the seventies by Helmut Busch, Hartha observatory, and later e.g. by Kh. F. Khaliullin, Moscow University, or J. V. Clausen, Copenhagen University (Wolf et al., 2004). A catalogue of eclipsing binaries that are suitable for photometric monitoring was provided by Hegedüs (2000) while a catalogue of known binaries with apsidal motion was published by Petrova & Orlov (1999).



**Fig. 3.**  $O - C$  residuals for the times of minimum of YY Sgr with respect to the linear part of the apsidal motion equation. (top). Below is the  $O - C_2$  diagram for the times of minimum of YY Sgr after subtraction the terms of the apsidal motion. The curve represents a light-time effect for the third body orbit with a period of 44 years with and an amplitude of about 0.008 days. (Wolf, 2000)

## The theory behind the effect

Suitable numerical methods for the apsidal motion analysis were described by Gimenez & García-Pelayo (1983), Lacy (1992), and Wolf & Šarounová (1995).

Below some basic concepts behind the core of the theory are provided just to recap of the method. There are five independent variables ( $T_0$ ,  $P_s$ ,  $e$ ,  $\omega_1$ ,  $\omega_0$ ) determined in this procedure.  $e$  represents the eccentricity of an orbit. The periastron position  $\omega$  at epoch  $E$  is defined by the famous linear equation:

$$\omega = \omega_0 + \omega_1 * E,$$

where  $\omega_1$  is the rate of periastron advance (in degrees per sidereal cycle or in degrees per year), and the position of periastron for the zero epoch  $T_0$  is denoted as  $\omega_0$ . On a shorter timescale, the precession of an eccentric orbit in its own plane can produce an observable rate of change in the longitude of periastron:

$$\omega_1 = d\omega / dt.$$

The sidereal and anomalistic periods of the binary,  $P_s$  and  $P_a$ , are connected by the following equation:

$$P_s = P_a (1 - \omega_1 / 360^\circ),$$

and the period of apsidal motion can be represented via

$$U = 360^\circ P_a / \omega_1$$

The rate of motion of the apsis is dependent on

## Eclipsing Binary with Eccentric Orbits Catalog

In 2007 there was a catalog containing a list of binary systems with eccentric orbits published (Bulut+). The catalog lists the physical parameters (including apsidal motion parameters) of 124 eclipsing binaries with eccentric orbits. In addition, the catalog also contains **a list of 150 candidate systems**, about which fewer details are known at present.

The catalog can be found at <http://cdsarc.u-strasbg.fr/viz-bin/Cat?J/MNRAS/378/179>

**J/MNRAS/378/179** - Eclipsing Binary with Eccentric Orbits Catalog (Bulut I., Demircan O., 2007)

## References for further reading:

- Giménez, A., García-Pelayo, J. M. 1983, Ap&SS, 92, 203
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the internal structure of each component. Determination of the characteristics of a binary thus provides an observational test of the theory of stellar structure and evolution. The apsidal motion in relatively close binary systems can be studied by means of an O–C diagram analysis (for details see, e.g., Wolf *et al.* 1996, 1997). See Fig.2 and Fig.3 as examples of this kind of research.

In the case of deep, narrow eclipses the rate of apsidal motion can be determined by the analysis of primary and secondary eclipse timings and by measuring the change in the displacement of the secondary minimum from the half point (0.5 phase) according to

$$D = (t_2 - t_1) - P / 2$$

where  $t_2$  and  $t_1$  are times of secondary and primary minima, respectively (GM85).  $D$ , in turn is related to the longitude of periastron  $\omega$  by the formula given by Sterne (1939, a, b):

$$D = \frac{P}{\pi} \left[ \tan^{-1} \left( \frac{e \cos \omega}{(1 - e^2)^{1/2}} \right) + \frac{e \cos \omega}{1 - e^2 \sin^2 \omega} (1 - e^2)^{1/2} \right]$$

For a short recap of the method: the individual equations for computing the time of primary and secondary minima are given in Giménez & García-Pelayo (1983). This is a weighted least squares iterative procedure, including terms in the eccentricity up to the fifth order.

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## Appendix 1. Examples of Eclipsing Binary Systems with Eccentric Orbits



V889 Aquilae, HD 181166



CW Cephei, SAO 20401



DI Herculis, SAO 86544



NY Cephei, SAO 20351



MZ Lacertae, SAO 12870



V402 Lacertae, SAO 51698



VW Pegasi, GSC 02753-00649



AR Cassiopeiae, SAO 35478

Object Designation		RA (J2000)	DEC (J2000)	Eccentricity	Period (days)	Mag. Range
<b>V889 Aql</b>	SAO 104708, HD 181166	19 18 49.8	+16 15 00	0.375	11.120879	8.52 - 9.1 V
<b>AR Cas</b>	SAO 35478, HIP 115990	23 30 01.9	+58 32 56	0.24	6.0663309	4.82 - 4.96 V
<b>CW Cep</b>	SAO 20401, HIP 113907	23 04 02.2	+63 23 48	0.29	2.72914	7.6 - 8.04 V
<b>EY Cep</b>	BD+80 112	03 40 04.0	+81 01 09	0.442	7.971438	9.8 - 10.57 V
<b>NY Cep</b>	SAO 20351, HIP 113461	22 58 39.8	+63 04 37	0.48	15.275727	7.4 - 7.55 V
<b>Alpha CrB</b>	SAO 83893, HIP 76267	15 34 41.3	+26 42 52	0.37	17.359907	2.21 - 2.32 B
<b>V541 Cyg</b>	GSC 02656-03703	19 42 29.4	+31 19 40	0.48	15.33779	10.2 - 10.9 p
<b>V1143 Cyg</b>	SAO 31850, HIP 96620	19 38 41.2	+54 58 25	0.54	7.6407613	5.85 - 6.37 V
<b>NN Del</b>	SAO 126201, HIP 102545	20 46 49.2	+07 33 10	0.518	99.2684	8.40 - 8.95 V
<b>DI Her</b>	SAO 86544, HIP 92708	18 53 26.2	+24 16 41	0.489	10.550168	8.39 - 9.11 V
<b>LV Her</b>	GSC 02076-01042	17 35 32.4	+23 10 30	0.61	18.435935	10.9 - 11.3 p
<b>MZ Lac</b>	SAO 12870, HIP 17257	22 28 01.7	+53 41 00	0.42	3.158795	11.2 - 12.1 p
<b>V345 Lac</b>	GSC 03986-02900	22 18 43.3	+54 40 33	0.456	7.491862	11.1 - 11.7 p
<b>V402 Lac</b>	SAO 51698, HIP 109354	22 09 15.2	+44 50 47	0.379	3.7820	6.7 - 6.99 Hp
<b>V2283 Sgr</b>	HD 321230	18 04 38.8	-36 54 52	0.488	3.4714231	10.23 - 11.03 V
<b>RU Mon</b>	BD-07 1623, HIP 33163	06 54 12.3	-07 35 45	0.396	3.584749	10.33 - 11.18 V
<b>FT Ori</b>	SAO 78120, HD 42858	06 13 58.1	+21 25 39	0.405	3.150415	9.1 - 9.9 V
<b>VW Peg</b>	GSC 02753-00649	22 56 23.6	+33 13 43	0.39	21.071749	9.9 - 10.6 V
<b>V436 Per</b>	SAO 22690, HIP 8704	01 51 59.3	+55 08 50	0.388	25.9359	5.49 - 5.85 V
<b>EQ Vul</b>	HD 337188, SON 4475	19 58 23.2	+28 01 08	0.359	9.297164	11.79 - 12.5 B